

LOG CALABI-YAU GEOMETRY AND CREMONA MAPS

ONLINE NOTTINGHAM ALGEBRAIC GEOMETRY SEMINAR

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3-DIMENSIONAL SCENARIO

VOLUME PRESERVING SARKISOV LINKS

Theorem (- 2023)

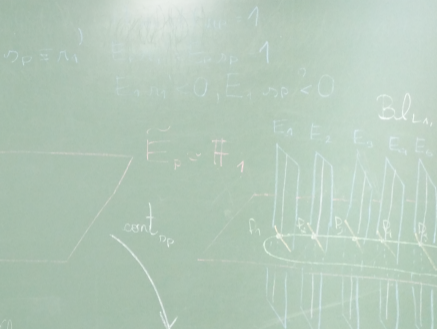
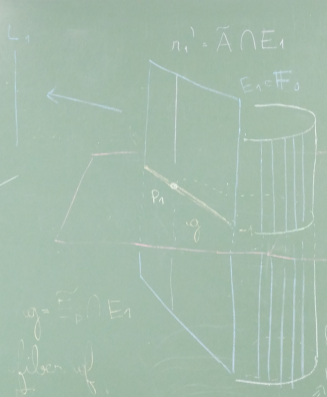
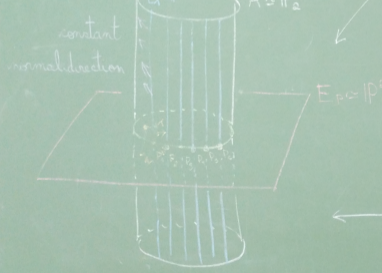
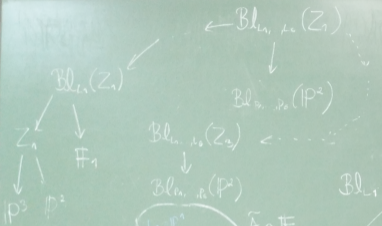
Let (\mathbb{P}^3, D) be a log Calabi-Yau pair of coregularity 2 and $\pi: (X, D_X) \rightarrow (\mathbb{P}^3, D)$ be a volume preserving toric $(1, a, b)$ -weighted blowup of a torus invariant point. Then this point is necessarily a singularity of D and, up to permutation, the only possibilities for the weights initiating a volume preserving Sarkisov link, depending on the type of singularities, are listed in the following table:

3-DIMENSIONAL SCENARIO

VOLUME PRESERVING SARKISOV LINKS

type of singularity	possible volume preserving weights
A_1	(1,1,1)
A_2	(1,1,1), (1,1,2)
A_3	(1,1,1), (1,1,2)
A_4	(1,1,1), (1,1,2), (1,2,3)
A_5	(1,1,1), (1,1,2), (1,2,3)
$A_{\geq 6}$	(1,1,1), (1,1,2), (1,2,3), (1,2,5)
D_4	(1,1,1), (1,1,2)
$D_{\geq 5}$	(1,1,1), (1,1,2), (1,2,3)
E_6	(1,1,1), (1,1,2), (1,2,3)
E_7	(1,1,1), (1,1,2), (1,2,3)
E_8	(1,1,1), (1,1,2), (1,2,3)

Table: Table summarizing volume preserving weights initiating Sarkisov links, up to permutation.



$g = \bar{E}_P \cap E_1$
 fiber of π_0
 $K_{Z_1} = \pi^* K_Z + 2E$
 $cD_2 = \pi^* D + cE$
 $K_{Z_2} = \pi^* K_{P^2} + 2E_P$
 $dZ_2 = \pi^* H - 2E_0$

THANK YOU!
OBRIGADO!

LMO