

**MATH1003  
ASSIGNMENT 7**

*Suggested practice questions (the answers are in the back of the textbook):*

- §3.5; 1, 3, 13, 25, 29.
- §3.6; 3, 17, 23, 37, 39.
- §3.11; 3, 9, 23, 31, 33.

1. (i) By using logarithmic differentiation, find  $\frac{dy}{dx}$  for  $y = (x + 2)^{10}(2x - 3)^4$ .  
(ii) Show that the derivative of:

$$y = \frac{(x + 1)^4}{\sqrt{x^2 - 1}}$$

is given by:

$$y' = \frac{(3x - 4)(x + 1)^4}{(x^2 - 1)^{3/2}}.$$

2. Find the derivative of the following functions:

- (i)  $y = e^{\cosh 3x}$ ,
- (ii)  $y = \sinh \cosh x$ ,
- (iii)  $y = x^2 \sinh^{-1} 2x$ ,
- (iv)  $y = \ln \sinh x$ .

3. Find an expression for  $\frac{dy}{dx}$  for the following curves. In each case, prove that the tangent to the curve is never parallel to the  $x$ -axis.

- (i)  $x^2 - y^2 = 1$ ,
- (ii)  $x^2 + y^2 = (1 + xy)^2$ .

4. (i) Let  $f(x) = 1/(5x - 1)$ . Find an expression for  $f^{(n)}$ , where  $n$  is a positive integer.  
(ii) Let  $h(\theta) = \theta e^{-\theta}$ . What is  $h^{(n)}(0)$ ?